

# ISC

## INDIAN SCHOOL CERTIFICATE EXAMINATION

### YEAR 2028



Empowering Minds & Transforming Lives since 1958

## APPLIED MATHEMATICS (885)

Developed by:  
Research, Development and Curriculum Division (RDCD)  
CISCE

January 2026

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## Council for the Indian School Certificate Examinations (CISCE)

### MISSION STATEMENT

*The Council for the Indian School Certificate Examinations is committed to serving the nation's children, through high quality educational endeavours, empowering them to contribute towards a humane, just and pluralistic society, promoting introspective living, by creating exciting learning opportunities, with a commitment to excellence.*

### ETHOS OF CISCE

- Trust and fair play.
- Minimum monitoring.
- Allowing schools to evolve their own niche.
- Catering to the needs of the children.
- Giving freedom to experiment with new ideas and practices.
- Diversity and plurality - the basic strength for evolution of ideas.
- Schools to motivate pupils towards the cultivation of:  
**Excellence** - The Indian and Global experience.  
**Values** - Spiritual and cultural - to be the bedrock of the educational experience.
- Schools to have an 'Indian Ethos', strong roots in the national psyche and be sensitive to national aspirations.

## APPLIED MATHEMATICS (885)

**This subject may not be taken with Mathematics.**

*(Note: For candidates who wish to pursue a career in Humanities/ Commerce/ Economics/ Biosciences/ Social Sciences and other related fields.)*

### **Aims**

1. To enable candidates to acquire knowledge and to develop an understanding of the terms, concepts, symbols, definitions, principles, processes and formulae of Mathematics at the Senior Secondary stage.
2. To develop the ability to apply the knowledge and understanding of Mathematics to unfamiliar situations or to new problems.
3. To enhance ability of analytical and rational thinking in young minds.
4. To develop mathematical thinking and ability to communicate mathematical ideas logically and precisely.
5. To develop skills of –
  - a. Computation.
  - b. Logical thinking.
  - c. Handling abstractions.
  - d. Generalising patterns.
  - e. Mathematical modeling to solve real-time problems.
  - f. Analysing the data and solving problems using multiple mathematical methods.
  - g. Reading and interpreting tables, charts, graphs, etc.
6. To enhance the ability to apply the mathematical skills in interdisciplinary subjects.
7. To develop an appreciation of the role of Mathematics in day-to-day life.
8. To develop a scientific attitude through the study of Mathematics.

# CLASS XI

There will be **two** papers in the subject:

**Paper I:** Theory (3 hours)...80 marks

**Paper II:** Project Work.....20 marks

## PAPER I (THEORY) : 80 MARKS

### DISTRIBUTION OF MARKS FOR THE THEORY PAPER

S.No	UNIT	TOTAL WEIGHTAGE
1.	Sets and Functions	12 Marks
2.	Algebra	22 Marks
3.	Coordinate Geometry	12 Marks
4.	Calculus	6 Marks
5.	Statistical methods & Probability	12 Marks
6.	Mathematical Reasoning	4 Marks
7.	Financial Mathematics	12 Marks
	<b>TOTAL</b>	<b>80 Marks</b>

#### 1. Sets and Functions

(i) Sets

Sets and their representations. Empty set. Finite and Infinite sets. Equal sets. Subsets. Subsets of a set of real numbers especially intervals (with notations). Power set. Universal set. Venn diagrams and practical applications. Union and Intersection of sets. Difference of sets. Symmetric Difference. Complement of a set. Properties of Complement of Sets. Algebra of sets.

- *Idempotent laws. Identity laws. Boundedness Laws.*
- *Commutative laws. Associative laws. Distributive laws.*
- *Laws of complementation.*
- *De Morgan's laws.*

(ii) Relations & Functions

Ordered pairs, Cartesian product of sets. Number of elements in the cartesian product of two finite sets. Cartesian product of the set of reals with itself. Definition of relation, pictorial diagrams, domain, co-domain and range of a relation. Function as a special type of relation. Function as a type of mapping, domain, co-domain and range of a function. Real valued functions, domain and range of these functions, constant, identity, polynomial, rational, modulus, signum, exponential, logarithmic and greatest integer functions. Sum, difference, product and quotient of functions.

- *Sets: Self-explanatory.*
- **Basic concepts of Relations and Functions**
  - *Ordered pairs, sets of ordered pairs.*
  - *Cartesian Product (Cross) of two sets, cardinal number of a cross product.*

*Relations as:*

- *an association between two sets.*
- *a subset of a Cross Product.*
- *Domain, Range and Co-domain of a Relation.*

*Functions:*

- *As special relations, concept of writing “y is a function of x” as  $y = f(x)$ .*
- *Domain and range of a function*
- *Reading, sketching and understanding the graphs of all standard real valued functions.*

(iii) Trigonometry

Positive and negative angles. Measuring angles in radians and in degrees and conversion from one measure to another. Definition of trigonometric functions with the help of unit circle. Truth of the identity  $\sin^2x + \cos^2x = 1$ , for all  $x$ . Signs of trigonometric functions. Domain and range of trigonometric functions and their graphs. Expressing  $\sin(x \pm y)$  and  $\cos(x \pm y)$  in terms of  $\sin x$ ,  $\sin y$ ,  $\cos x$  &  $\cos y$  and their simple applications. Deducing the identities like the following:

$$\tan(x \pm y) = \frac{\tan x \pm \tan y}{1 \mp \tan x \tan y},$$

$$\cot(x \pm y) = \frac{\cot x \cot y \mp 1}{\cot y \pm \cot x}$$

$$\sin \alpha \pm \sin \beta = 2 \sin \frac{1}{2}(\alpha \pm \beta) \cos \frac{1}{2}(\alpha \mp \beta)$$

$$\cos \alpha + \cos \beta = 2 \cos \frac{1}{2}(\alpha + \beta) \cos \frac{1}{2}(\alpha - \beta)$$

$$\cos \alpha - \cos \beta = -2 \sin \frac{1}{2}(\alpha + \beta) \sin \frac{1}{2}(\alpha - \beta)$$

Identities related to  $\sin 2x$ ,  $\cos 2x$ ,  $\tan 2x$ ,  $\sin 3x$ ,  $\cos 3x$  and  $\tan 3x$ .

• **Angles and Arc lengths**

- *Angles: Convention of sign of angles.*
- *Magnitude of an angle: Measures of Angles; Circular measure.*
- *The relation  $S = r\theta$  where  $\theta$  is in radians. Relation between radians and degree.*
- *Definition of trigonometric functions with the help of unit circle.*
- *Truth of the identity  $\sin^2x + \cos^2x = 1$*

**NOTE:** Questions on the area of a sector of a circle are required to be covered.

• **Trigonometric Functions**

- *Relationship between trigonometric functions.*
- *Proving simple identities.*
- *Signs of trigonometric functions.*
- *Domain and range of the trigonometric functions.*
- *Trigonometric functions of all angles.*
- *Periods of trigonometric functions.*
- *Graphs of simple trigonometric functions (only sketches).*

**NOTE:** Graphs of  $\sin x$ ,  $\cos x$ ,  $\tan x$ ,  $\sec x$ ,  $\operatorname{cosec} x$  and  $\cot x$  are to be included.

- **Compound and multiple angles**

- Addition and subtraction formula:  $\sin(A \pm B)$ ;  $\cos(A \pm B)$ ;  $\tan(A \pm B)$ ;  $\tan(A + B + C)$  etc., Double angle, triple angle, half angle and one third angle formula as special cases.
- Sum and differences as products i.e.  $\sin C + \sin D = 2\sin\left(\frac{C+D}{2}\right)\cos\left(\frac{C-D}{2}\right)$ , etc.
- Product to sum or difference i.e.  $2\sin A \cos B = \sin(A+B) + \sin(A-B)$  etc.
- **Simple problems based on above concepts**

## 2. Algebra

(i) Logarithm

Introduction and definition of logarithm and anti-logarithm.

*Properties: Common & Natural logarithms*

*Problems based on logarithm and anti-logarithm.*

(ii) Complex Numbers

Introduction of complex numbers and their representation, Algebraic properties of complex numbers. Argand plane and polar representation of complex numbers.

- *Conjugate, modulus and argument of complex numbers and their properties.*
- *Sum, difference, product and quotient of two complex numbers, additive and multiplicative inverse of a complex number.*

(iii) Quadratic Equations

Statement of Fundamental Theorem of Algebra, solution of quadratic equations (with real coefficients).

- *Use of the formula:*

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

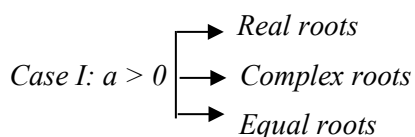
*In solving quadratic equations.*

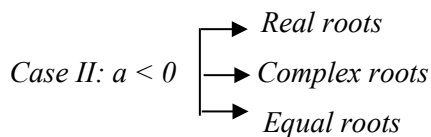
- *Equations reducible to quadratic form.*
- *Nature of roots*
  - *Product and sum of roots.*
  - *Roots are rational, irrational, equal, reciprocal, one square of the other.*
  - *Complex roots.*
  - *Framing quadratic equations with given roots.*

**NOTE:** *Questions on equations having common roots are to be covered.*

- **Quadratic Functions.**

*Given  $\alpha, \beta$  as roots then find the equation whose roots are of the form  $\alpha^3, \beta^3$ , etc.*





Where 'a' is the coefficient of  $x^2$  in the equations of the form  $ax^2 + bx + c = 0$ .

- **Sign of quadratic**

Sign when the roots are real and when they are complex.

- Graph of quadratic function. Maximum/minimum value of quadratic function and value of  $x$  for which maximum/minimum occurs.

- **Inequalities**

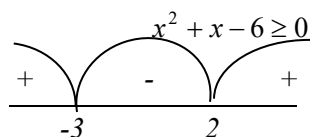
- Linear Inequalities

Algebraic solutions of linear inequalities in one variable and their representation on the number line.

Self-explanatory.

- Quadratic Inequalities

Using method of intervals for solving problems of the type:



A perfect square e.g.  $x^2 - 6x + 9 \geq 0$ .

(iv) Permutations and Combinations

Fundamental principle of counting. Factorial  $n$ . ( $n!$ ) Permutations and combinations, derivation of formulae for  ${}^n P_r$  and  ${}^n C_r$  and their connections, simple application.

- Factorial notation  $n!$ ,  $n! = n(n-1)!$
- Fundamental principle of counting.
- Permutations
  - ${}^n P_r$ .
  - Restricted permutation.
  - Certain things always occur together.
  - Certain things never occur.
  - Formation of numbers with digits.
  - Word building - repeated letters - No letters repeated.
  - Permutation of alike things.
  - Permutation of Repeated things.
  - Circular permutation – clockwise counterclockwise – Distinguishable / not distinguishable.
- Combinations
  - ${}^n C_r, {}^n C_n = 1, {}^n C_0 = 1, {}^n C_r = {}^n C_{n-r}, {}^n C_x = {}^n C_y$ , then  $x + y = n$  or  $x = y, {}^{n+1} C_r = {}^n C_{r-1} + {}^n C_r$ .
  - Total number of combinations of  $n$  dissimilar things taking any number of them at a time
    - When all things are different.
    - When all things are not different.
  - Division, distribution into groups.

- Mixed problems on permutation and combinations.

(v) Binomial Theorem

History, statement of the binomial theorem for positive integral indices.

Pascal's triangle, General and middle term(s) in binomial expansion, simple applications.

- Significance of Pascal's triangle.
- Binomial theorem for positive integral powers,

$$\text{i.e. } (x + y)^n = {}^nC_0x^n + {}^nC_1x^{n-1}y + \dots + {}^nC_ny^n.$$

- Binomial coefficients.  
Questions based on the above.

(vi) Sequence and Series.

Sequence and Series. Arithmetic Progression (A.P.). Arithmetic Mean (A.M.) Geometric Progression (G.P.), general term of a G.P., sum of first  $n$  terms of a G.P., infinite G.P. and its sum, geometric mean (G.M.), relation between A.M. and G.M. Formulae for the following special sums  $\sum n, \sum n^2, \sum n^3$ .

- Arithmetic Progression (A.P.)

-  $T_n = a + (n - 1)d$

-  $S_n = \frac{n}{2} \{2a + (n - 1)d\}$

- Arithmetic mean:  $2b = a + c$

- Inserting two or more arithmetic means between any two numbers.

- Three terms in A.P. :  $a - d, a, a + d$

- Four terms in A.P.:  $a - 3d, a - d, a + d, a + 3d$

- Geometric Progression (G.P.)

-  $T_n = ar^{n-1}$ ,

-  $S_n = \frac{a(r^n - 1)}{r - 1}, |r| > 1, \quad S_n = \frac{a(1 - r^n)}{1 - r}, |r| < 1$

-  $S_\infty = \frac{a}{1 - r}; |r| < 1$

- Geometric Mean,  $b = \sqrt{ac}$

- Inserting two or more Geometric Means between any two numbers.

- Three terms are in G.P.  $ar, a, ar^{-1}$

- Four terms are in GP  $ar^3, ar, ar^{-1}, ar^{-3}$

- Special sums  $\sum n, \sum n^2, \sum n^3$

Using these summations to sum up other related expression.

Finding  $n^{\text{th}}$  term of a sequence using Method of difference.

### 3. Coordinate Geometry

#### (i) Straight Lines

Brief recall of two-dimensional geometry from earlier classes. Shifting of origin. Slope of a line and angle between two lines. Various forms of equations of a line: parallel to axis, point-slope form, slope-intercept form, two-point form, intercept form and normal form. General equation of a line. Equation of family of lines passing through the point of intersection of two lines. Distance of a point from a line.

- *Brief recall of basic concepts of Points and their coordinates.*
  - *Section formula (internally/externally)*
  - *Coordinates of incentre, Area of triangle when vertices are given*
  - *Condition for collinearity of three points*
- *The straight line*
  - *Slope or gradient of a line.*
  - *Angle between two lines.*
  - *Condition of perpendicularity and parallelism.*
  - *Various forms of equation of lines.*
  - *Slope intercept form.*
  - *Two-point slope form.*
  - *Intercept form.*
  - *Perpendicular /normal form.*
  - *General equation of a line.*
  - *Distance of a point from a line.*
  - *Distance between parallel lines.*
  - *Equation of lines bisecting the angle between two lines.*
  - *Equation of family of lines*
  - *Definition of a locus.*
  - *Equation of a locus.*

#### (ii) Circles

- *Equations of a circle in:*
  - *Standard form.*
  - *Diameter form.*
  - *General form.*
  - *Parametric form.*
- *Given the equation of a circle, to find the centre and the radius.*
- *Finding the equation of a circle.*
  - *Given three non collinear points.*
  - *Given other sufficient data for example centre is  $(h, k)$  and it lies on a line and two points on the circle are given, etc.*

#### (iii) Parabola

Standard equations and simple properties of parabola.

- *Conics as a section of a cone.*
  - *Definition of Foci, Directrix, Latus Rectum.*

- $PS = ePL$  where  $P$  is a point on the conics,  $S$  is the focus,  $PL$  is the perpendicular distance of the point from the directrix.
- *Parabola*
  - $e = 1, y^2 = 4ax, x^2 = 4ay, y^2 = -4ax, x^2 = -4ay.$
  - *Rough sketch of the above.*
  - *The latus rectum; quadrants they lie in; coordinates of focus and vertex; and equations of directrix and the axis.*
  - *Finding equation of Parabola when Foci and directrix are given, etc.*
  - *Application questions based on the above.*

#### 4. Calculus

##### (i) Limits and Derivatives

Derivative introduced as rate of change both as that of distance function and geometrically. Intuitive idea of limit. Limits of polynomials and rational functions trigonometric, exponential and logarithmic functions. Definition of derivative, relate it to slope of tangent of the curve, Derivative of sum, difference, product and quotient of functions. Derivatives of polynomial and trigonometric functions.

- *Limits*
  - *Notion and meaning of limits.*
  - *Fundamental theorems on limits (statement only).*
  - *Existence of  $\lim_{x \rightarrow a} f(x)$*
  - *Left hand limit, Right hand limit.*
  - *Limits of algebraic, trigonometric, exponential, and logarithmic functions.*

**NOTE:** Indeterminate forms are to be introduced while calculating limits.

- *Differentiation*
  - *Meaning and geometrical interpretation of derivative.*
  - *Derivatives of simple algebraic and trigonometric functions and their formulae.*
  - *Differentiation using first principles.*
  - *Derivatives of sum/difference.*
  - *Derivatives of product of functions.*
  - *Derivatives of quotients of functions.*

#### 5. Statistical Methods and Probability

##### Statistical Methods

##### (i) Measures of dispersion

Measures of dispersion: range, mean deviation, variance and standard deviation of ungrouped/grouped data.

- *Range*
- *Quartiles, Interquartile range, Quartile deviation, Coefficient of Quartile deviation*
- *Mean deviation about mean and median, coefficient of mean deviation*
- *Mean deviation about median.*
- *Standard deviation - by direct method, short cut method and step deviation method, Variance and coefficient of variance*
- *Combined mean and standard deviation*

- *Mode of grouped and ungrouped data.*
- *Differentiate between range, quartile deviation, mean deviation and standard deviation.*
- *Choose appropriate measure of dispersion to calculate spread of data.*

(ii) Skewness and Kurtosis:

- *Define Skewness and Kurtosis using graphical representation of a data set.*
- *Interpret Skewness and Kurtosis of a frequency distribution by plotting the graph.*
- *Calculate coefficient of Skewness and interpret the results.*
- *Empirical Relation between Mean, Median and Mode*
- *Moments*
- *Measures of skewness – Absolute and Relative*
- *Relative measures –*
  - *Karl Pearson's Coefficient of Skewness.*
  - *Bowley's Coefficient of Skewness.*
  - *$\beta$  and  $\gamma$  Coefficient of Skewness*
- *Karl Pearson's Measures of Kurtosis*

(iii) Correlation Analysis

- *Definition and meaning of covariance.*
- *Coefficient of Correlation by Karl Pearson.*

*If  $x - \bar{x}$ ,  $y - \bar{y}$  are small non - fractional numbers, we use*

$$r = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sqrt{\sum(x - \bar{x})^2} \sqrt{\sum(y - \bar{y})^2}}$$

*If  $x$  and  $y$  are small numbers, we use*

$$r = \frac{\sum xy - \frac{1}{N} \sum x \sum y}{\sqrt{\sum x^2 - \frac{1}{N} (\sum x)^2} \sqrt{\sum y^2 - \frac{1}{N} (\sum y)^2}}$$

*Otherwise, we use assumed means*

*$A$  and  $B$ , where  $u = x - A$ ,  $v = y - B$*

$$r = \frac{\sum uv - \frac{1}{N} (\sum u)(\sum v)}{\sqrt{\sum u^2 - \frac{1}{N} (\sum u)^2} \sqrt{\sum v^2 - \frac{1}{N} (\sum v)^2}}$$

- *Differentiate between causation and correlation.*
- *Rank Correlation by Spearman's (Correction included)*

(iv) Linear Regression

- Lines of regression of x on y and y on x.
- Scatter diagrams.
- The method of least squares.
- Lines of best fit.
- Regression coefficient of x on y and y on x.
- $b_{xy} \times b_{yx} = r^2$  ,  $0 \leq b_{xy} \times b_{yx} \leq 1$
- Identification of regression equations.
- Properties of regression lines.
- Estimation of the value of one variable using the value of other variable from appropriate line of regression.

*Self-explanatory*

(v) Probability

Random experiments; outcomes, sample spaces (set representation). Events; occurrence of events, 'not', 'and' and 'or' events, exhaustive events, mutually exclusive events, Axiomatic (set theoretic) probability, connections with other theories studied in earlier classes. Probability of an event, probability of 'not', 'and' and 'or' events.

- *Random experiments and their outcomes.*
- *Events: sure events, impossible events, mutually exclusive and exhaustive events.*
  - *Definition of probability of an event*
  - *Laws of probability addition theorem.*

## 6. Mathematical Reasoning

- (i) Mathematically acceptable statements. Connecting words/ phrases - consolidating the understanding of "if and only if (necessary and sufficient) condition", "implies", "and/or", "implied by", "and", "or", "there exists" and their use through variety of examples related to the Mathematics and real life. Validating the statements involving the connecting words (*Truth tables*), Difference between contradiction, converse and contrapositive.

*Creating natural data set using random experiment such as tossing a coin multiple times.*

- (ii) Logical problems involving odd man out, syllogism, blood (family) relation and coding decoding.

## 7. Financial Mathematics

- (i) Interest and Interest Rates: Define the concept of Interest Rates (simple and compound). Compare the difference between Nominal Interest Rate, Effective Rate and Real Interest Rate, Concept of equivalency. Compounding Frequency.

- *APR (Annual Percentage Rate)*
- *AER (Annual Equivalent Rate).*
- *Annualised Yield*

- (ii) Present value, net present value and future value: Interpret the concept of compounding and discounting along with practical applications. Compute net present value. Apply net present value in capital budgeting decisions

- (iii) Annuities, Calculating value of Regular Annuity: Immediate Annuity, Annuity due and Deferred Annuity. General Annuity. Calculate the future value of regular annuity, annuity due. Apply the concept of Annuity in real life situations.
- (iv) Fundamentals of Taxation: Differentiate between Direct and indirect tax. Define, explain and calculate GST. Explain rules under SGST, CGST, and UTGST.
- (v) Bills, tariff rates, fixed charge, surcharge, service charge: Interpret and analyse electricity bills, water bills and other supply bills.

## PAPER II (PROJECT WORK) : 20 MARKS

Candidates will be expected to have completed **two** projects

Mark allocation for **each** Project [10 marks]:

Overall format	1 mark
Content	4 marks
Findings	2 marks
Viva-voce based on the Project	3 marks
<b>Total</b>	<b>10 marks</b>

### List of suggested assignments for Project Work:

- Explore different methods to prove the result “If a set has ‘n’ number of elements, then the total number of subsets is  $2^n$ ”.
- Verify that for two sets A and B,  $n(A \times B) = pq$ , where  $n(A) = p$  and  $n(B) = q$ , the total number of relations from A to B is  $2^{pq}$ .
- Using Venn diagram, verify the distributive law for three given non-empty sets A, B and C.
- Identify distinction between a relation and a function with suitable examples and illustrate graphically.
- Establish the relationship between the measure of an angle in degrees and in radians with suitable examples by drawing a rough sketch.
- Illustrate with the help of a model, the values of sine and cosine functions for different angles which are multiples of  $\pi/2$  and  $\pi$ .
- Draw the graphs of  $\sin x$ ,  $\sin 2x$ ,  $2 \sin x$ , and  $\sin x/2$  on the same graph using same coordinate axes and interpret the same.
- Draw the graph of  $\cos x$ ,  $\cos 2x$ ,  $2 \cos x$ , and  $\cos x/2$  on the same graph using same coordinate axes and interpret the same.
- Using argand plane, interpret geometrically, the meaning of  $i = \sqrt{-1}$  and its integral powers.
- Draw the graph of quadratic function  $f(x) = ax^2 + bx + c$ . From the graph find maximum/minimum value of the function. Also determine the sign of the expression.
- Construct a Pascal’s triangle to write a binomial expansion for a given positive integral exponent.
- Obtain a formula for the sum of the squares/sum of cubes of ‘n’ natural numbers.
- Obtain the equation of the straight line in the normal form, for  $\alpha$  (the angle between the perpendicular to the line from the origin and the x-axis) for each of the following, on the same graph:
  - $\alpha < 90^\circ$

- (ii)  $90^\circ < \alpha < 180^\circ$
  - (iii)  $180^\circ < \alpha < 270^\circ$
  - (iv)  $270^\circ < \alpha < 360^\circ$
14. Identify the variability and consistency of two sets of statistical data using the concept of coefficient of variation.
  15. Construct the tree structure of the outcomes of a random experiment, when elementary events are not equally likely. Also construct a sample space by taking a suitable example.
  16. Let  $S$  and  $S_1$  be two (non-concentric) circles with centres  $A$ ,  $B$  and radii  $r_1$ ,  $r_2$  and  $d$  be the distance between their centres. Relation between  $r_1$ ,  $r_2$  and  $d$  with respect to relative position of two circles.
  17. Obtain truth values of compound statements of the type  $p \wedge q$  by using switch connection in series.
  18. Obtain truth values of compound statements of the type  $p \vee q$  by using switch connection in parallel.
  19. Explain the statistical significance of percentile and draw inferences of percentile for a given data.
  20. Find median from the point of intersection of cumulative frequency curves (less than and more than cumulative frequency curves).
  21. Describe the limitations of Spearman's rank correlation coefficient and illustrate with suitable examples.
  22. Correlation between the height of the student and the proficiency in long jump.
  23. Correlation between monthly income and education qualification.
  24. Correlation between sleeping disorder and the usage of smart phone.
  25. Correlation between the particular disease (like varicose vein pain/ back ache /migraine) and the profession of the patient.
  26. Smart purchasing during sale season.
  27. Prepare the best option plan to buy a product by comparing cost, shipping charges, tax (under GST), and hidden cost, overhead cost etc.

## CLASS XII

There will be **two** papers in the subject:

**Paper I:** Theory (3 hours) ...80 marks

**Paper II:** Project Work.....20 marks

### PAPER I (THEORY) : 80 MARKS

**Distribution of marks for the theory paper:**

S.No.	UNIT	TOTAL WEIGHTAGE
1.	Relations and Functions	6 Marks
2.	Algebra	10 Marks
3.	Calculus	25 Marks
4.	Probability	14 Marks
5.	Linear Programming	5 Marks
6.	Financial Mathematics	14 Marks
7.	Index numbers & Moving averages	6 Marks
	<b>TOTAL</b>	<b>80 Marks</b>

#### 1. Relations and Functions

(i) Types of relations: reflexive, symmetric, transitive and equivalence relations. One to one and onto functions, composite function and inverse of a function.

- *Relations as:*
  - *Relation on a set A*
  - *Identity relation, empty relation, universal relation.*
  - *Types of Relations: reflexive, symmetric, transitive and equivalence relation.*
- *Functions:*
  - *As special relations, concept of writing “y is a function of x” as  $y = f(x)$ .*
  - *Types: one to one, many to one, into, onto.*
  - *Real Valued function.*
  - *Domain and range of a function.*
  - *Conditions of invertibility.*
  - *Sketching of graph of a function and its inverse.*
  - *Composite functions and Invertible functions (algebraic functions only).*

(ii) Inverse Trigonometric Functions

Definition, domain, range, principal value branch. Graphs of inverse trigonometric functions. Elementary properties of inverse trigonometric functions.

- *Principal values.*
- *$\sin^{-1}x, \cos^{-1}x, \tan^{-1}x$  etc.*
- $\sin^{-1}x = \cos^{-1}\sqrt{1-x^2} = \tan^{-1}\frac{x}{\sqrt{1-x^2}}.$

- $\sin^{-1}x = \operatorname{cosec}^{-1} \frac{1}{x}$ ;  $\sin^{-1}x + \cos^{-1}x = \frac{\pi}{2}$  and similar relations for  $\cot^{-1}x$ ,  $\tan^{-1}x$ , etc.

## 2. Algebra

### Matrices and Determinants

#### (i) Matrices

Concept, notation, order, equality, types of matrices, zero and identity matrix, transpose of a matrix, symmetric and skew symmetric matrices. Operation on matrices: Addition and multiplication and multiplication with a scalar. Simple properties of addition, multiplication and scalar multiplication. Non-commutativity of multiplication of matrices and existence of non-zero matrices whose product is the zero matrix (restrict to square matrices of order upto 3). Invertible matrices and proof of the uniqueness of inverse, if it exists (here all matrices will have real entries).

#### (ii) Determinants

Determinant of a square matrix (up to  $3 \times 3$  matrices), minors, co-factors and applications of determinants in finding the area of a triangle. Adjoint and inverse of a square matrix. Consistency, inconsistency and number of solutions of system of linear equations by examples, solving system of linear equations in two or three variables (having unique solution) using inverse of a matrix/Cramer's Rule.

- *Types of matrices ( $m \times n$ ;  $m, n \leq 3$ ), order; Diagonal matrix, Scalar matrix, Identity matrix, Triangular matrix.*
- *Symmetric, Skew symmetric matrices. Properties of Symmetric, Skew symmetric matrices.*
- *Operation – addition, subtraction, multiplication of a matrix with scalar, multiplication of two matrices (the compatibility).*

$$\text{E.g. } \begin{bmatrix} 1 & 1 \\ 0 & 2 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 2 & 2 \end{bmatrix} = AB(\text{say}) \text{ but } BA \text{ is not possible.}$$

- *Singular and non-singular matrices.*
- *Existence of two non-zero matrices whose product is a zero matrix.*
- *Properties of adjoint of a square matrix.*
- *Inverse ( $2 \times 2$ ,  $3 \times 3$ )  $A^{-1} = \frac{\operatorname{Adj}A}{|A|}$*

- *Properties of inverse*

#### • *Martin's Rule (i.e. using matrices)*

$$a_1x + b_1y + c_1z = d_1$$

$$a_2x + b_2y + c_2z = d_2$$

$$a_3x + b_3y + c_3z = d_3$$

$$A = \begin{bmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{bmatrix} \quad B = \begin{bmatrix} d_1 \\ d_2 \\ d_3 \end{bmatrix} \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$AX = B \Rightarrow X = A^{-1}B$$

*Problems based on above.*

**NOTE:** The conditions for consistency of equations in two and three variables, using matrices/determinants, are to be covered.

- *Determinants*
  - *Order.*
  - *Minors.*
  - *Cofactors.*
  - *Expansion.*
  - *Applications of determinants in finding the area of triangle and collinearity.*
  - *Cramer's rule: Solving system of equations of two/three variables.*

### 3. Calculus

- (i) Differentiation, derivative of composite functions, chain rule, derivatives of inverse trigonometric functions, derivative of implicit functions.

Derivatives of logarithmic and exponential functions. Logarithmic differentiation, derivative of functions expressed in parametric forms. Second order derivatives.

Rate of change, Increasing/ decreasing functions, maxima and minima.

- *Differentiation*
  - *Derivatives of trigonometric and inverse trigonometric functions.*
  - *Derivatives of exponential functions.*
  - *Derivatives of logarithmic functions.*
  - *Derivatives of implicit functions and chain rule.*
  - *Derivatives of Parametric functions.*
  - *Differentiation of a function with respect to another function e.g. differentiation of  $\sin x^3$  with respect to  $x^3$ .*
  - *Logarithmic Differentiation - Finding  $dy/dx$  when  $y = x^{x^{x^{\dots}}}$ .*
  - *Successive differentiation up to 2<sup>nd</sup> order.*

**NOTE:** Derivatives of composite functions using chain rule.

- *Rate measure.*
- *Increasing and decreasing functions.*
- *Maxima and minima.*
  - *Stationary /turning points,*
  - *First derivatives test and second derivatives test*

- (ii) Integrals

Integration as inverse process of differentiation. Integration of a variety of functions by substitution, by partial fractions and by parts, Evaluation of simple integrals of the following types and problems based on them.

Fundamental Theorem of Calculus (without proof). Basic properties of definite integrals and evaluation of definite integrals.

- **Indefinite integral**

- Integration as the inverse of differentiation (anti-derivative).
- Anti-derivatives of polynomials and functions  $(ax + b)^n$ ,  $\sin x$ ,  $\cos x$ ,  $\sec^2 x$ ,  $\operatorname{cosec}^2 x$  etc .
- Integrals of the type  $\sin^2 x$ ,  $\sin^3 x$ ,  $\sin^4 x$ ,  $\cos^2 x$ ,  $\cos^3 x$ ,  $\cos^4 x$ .
- Integration of  $1/x$ ,  $e^x$ .
- Integration by substitution.
- Integrals of the type  $f'(x)[f(x)]^n$ ,  $\frac{f'(x)}{f(x)}$ .
- Integration of  $\tan x$ ,  $\cot x$ ,  $\sec x$ ,  $\operatorname{cosec} x$ .
- Integration by parts.
- Integration using partial fractions.

Expressions of the form  $\frac{f(x)}{g(x)}$  when degree of  $f(x) <$  degree of  $g(x)$

$$\text{E.g. } \frac{x+2}{(x-3)(x+1)} = \frac{A}{x-3} + \frac{B}{x+1}$$

$$\frac{x+2}{(x-2)(x-1)^2} = \frac{A}{x-1} + \frac{B}{(x-1)^2} + \frac{C}{x-2}$$

$$\frac{x+1}{(x^2+3)(x-1)} = \frac{Ax+B}{x^2+3} + \frac{C}{x-1}$$

When degree of  $f(x) \geq$  degree of  $g(x)$ , e.g.  $\frac{x^2+1}{x^2+3x+2} = 1 - \left( \frac{3x+1}{x^2+3x+2} \right)$

- Integrals of the type:

$$\int \frac{dx}{x^2 \pm a^2}, \int \frac{dx}{\sqrt{x^2 \pm a^2}}, \int \frac{px+q}{ax^2+bx+c} dx, \int \frac{px+q}{\sqrt{ax^2+bx+c}} dx$$

- **Definite Integral**

- Fundamental theorem of calculus (without proof)
- Properties of definite integrals.
- Problems based on the following properties of definite integrals are to be covered.

$$\int_a^b f(x) dx = \int_a^b f(t) dt$$

$$\int_a^b f(x) dx = - \int_b^a f(x) dx$$

$$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx \quad \text{where } a < c < b$$

$$\int_a^b f(x)dx = \int_a^b f(a+b-x)dx$$

$$\int_0^a f(x)dx = \int_0^a f(a-x)dx$$

$$\int_0^{2a} f(x)dx = \begin{cases} 2\int_0^a f(x)dx, & \text{if } f(2a-x) = f(x) \\ 0, & \text{if } f(2a-x) = -f(x) \end{cases}$$

$$\int_{-a}^a f(x)dx = \begin{cases} 2\int_0^a f(x)dx, & \text{if } f \text{ is an even function} \\ 0, & \text{if } f \text{ is an odd function} \end{cases}$$

(iii) Application of Calculus in Commerce and Economics in the following:

- Cost function,
- average cost,
- marginal cost and its interpretation
- demand function,
- revenue function,
- marginal revenue function and its interpretation,
- Profit function and breakeven point.
- Rough sketching of the following curves: AR, MR, R, C, AC, MC and their mathematical interpretation using the concept of maxima & minima and increasing- decreasing functions.
- Identify the region representing C.S. and P.S. graphically. Apply the definite integral to find consumer surplus-producer surplus, etc.
- Problems based on finding -Total cost when Marginal Cost is given - Total Revenue when Marginal Revenue is given -Equilibrium price and equilibrium quantity and hence consumer and producer surplus etc.

*Self-explanatory*

**NOTE: Application involving differentiation, increasing and decreasing function and maxima and minima to be covered.**

**Application involving integration, definite integration to be covered.**

(iv) Differential Equations

Definition, order and degree, general and particular solutions of a differential equation. Solution of differential equations by method of separation of variables.

- *Differential equations, order and degree.*
- *Formation of differential equation by eliminating arbitrary constant(s).*
- *Solution of differential equations.*
- *Variable separable.*
- *Homogeneous equations.*

- Linear form  $\frac{dy}{dx} + Py = Q$ , where  $P$  and  $Q$  are functions of  $x$ /constant. Similarly, for  $dx/dy$ .

**NOTE 1:** Equations reducible to variable separable type are included.

**NOTE 2:** The second order differential equations are excluded.

#### 4. Probability

Conditional probability, multiplication theorem on probability, independent events, total probability, Bayes' theorem, Random variable and its probability distribution, mean and variance of random variable. Binomial, Poisson and Normal distributions and its application in real life situation. Advantages & disadvantages of each type of distributions.

- *Independent and dependent events conditional events.*
- *Laws of Probability, addition theorem, multiplication theorem, conditional probability.*
- *Theorem of Total Probability.*
- *Bayes' theorem.*
- *Theoretical probability distribution, probability distribution function; mean and variance of random variable.*
- *Binomial distribution*
  - *Bernoulli's trials.*
  - *Binomial distribution*
  - *Mean and variance*
- *Poisson Distribution*
  - *Definition of Poisson distribution*
  - *Characteristics*
  - *Mean and variance*
- *Normal distribution*
  - *Concept of continuous of distribution*
  - *Understanding the normal distribution is a Continuous distribution.*
  - *Standard normal variate*
  - *Mean and Standard deviation.*
  - *Total area under the curve*
  - *Area relationship between Mean and Standard deviation.*

#### 5. Linear Programming

Introduction, related terminology such as constraints, objective function, optimization, different types of linear programming (L.P.) problems, mathematical formulation of L.P. problems, graphical method of solution for problems in two variables, feasible (bounded and unbounded) and infeasible regions, feasible and infeasible solutions, optimal feasible solutions (up to three non-trivial constraints).

- *Introduction, definition of related terminology such as constraints, objective function, optimization, advantages of linear programming; limitations of linear programming; application areas of linear programming; different types of linear programming (L.P.) problems, mathematical formulation of L.P. problems, graphical method of solution for problems in two variables, feasible (bounded/ unbounded) and infeasible regions, feasible and infeasible solutions, optimum feasible solution(may/may not exists).*

## 6. Financial Mathematics

- Perpetuity, Sinking Funds (Meaning). Real life examples of sinking fund. Advantages of sinking fund. Sinking fund vs. Savings account.
- EMI (Methods to calculate EMI (Flat rate method, Reducing balance method). Real life examples to calculate EMI of various types of loans, purchase of assets etc.
- Rate of Return, Nominal rate of return (meaning and use) and their formula.
- Compound Annual Growth Rate (Meaning and use) and their formula.
- Linear Method of Depreciation (Meaning) and its formula. Advantages and disadvantages of Linear Method.

## 7. Index Numbers and Moving Averages

### (i) Index Numbers

- *Price index or price relative.*
- *Simple average of price relatives.*
- *Weighted average of price relatives (cost of living index, consumer price index).*
- *Simple aggregate method.*
- *All types of weighted aggregate index number methods and their advantages/disadvantages with reference to real life situation.*

### (ii) Moving Averages

- *Meaning and purpose of the moving averages.*
- *Calculation of moving averages with the given periodicity and plotting them on a graph.*

*If the period is even, then the centered moving average is to be found out and plotted.*

## PAPER II (PROJECT WORK) : 20 MARKS

Candidates will be expected to have completed **two projects**. The project work will be assessed by the subject teacher and a Visiting Examiner appointed locally and approved by the Council.

Mark allocation for **each** Project [10 marks]:

Overall format	1 mark
Content	4 marks
Findings	2 marks
Viva-voce based on the Project	3 marks
<b>Total</b>	<b>10 marks</b>

### List of suggested assignments for Project Work:

1. Using a graph, demonstrate a function which is one-one but not onto.
2. Using a graph demonstrate a function which is invertible.
3. Draw the graph of  $y = \sin^{-1} x$  (or any other inverse trigonometric function), using the graph of  $y = \sin x$  (or any other relevant trigonometric function). Demonstrate the concept of mirror line (about  $y = x$ ) and find its domain and range.
4. Explore the principal value of the function  $\sin^{-1} x$  (or any other inverse trigonometric function) using a unit circle.
5. Find the derivatives of a determinant of the order of  $3 \times 3$  and verify the same by other methods.
6. Verify the consistency of the system of three linear equations of two variables and verify the same graphically. Give its geometrical interpretation.
7. For a dependent system (non-homogeneous) of three linear equations of three variables, identify infinite number of solutions.
8. Explain the concepts of increasing and decreasing functions, using geometrical significance of  $dy/dx$ . Illustrate with proper examples.
9. Explain and illustrate (with suitable examples) the concept of local maxima and local minima using graph.
10. Explain the conditional probability, the theorem of total probability and the concept of Bayes' theorem with suitable examples.
11. Explain the types of probability distributions and derive mean and variance of binomial probability distribution for a given function.
12. Using any suitable data, find the minimum cost by applying the concept of Transportation problem.
13. Using any suitable data, find the minimum cost and maximum nutritional value by applying the concept of Diet problem.
14. Using any suitable data, find the Optimum cost in the manufacturing problem by formulating a linear programming problem (LPP).
15. Draw a rough sketch of Cost (C), Average Cost (AC) and Marginal Cost (MC)

Or

Revenue (R), Average Revenue (AR) and Marginal Revenue (MR).

Give their mathematical interpretation using the concept of increasing - decreasing functions and maxima-

minima.

16. Different methods to calculate depreciation. Main inputs to calculate depreciation. Linear or straight line method to find depreciation with a suitable real life example.
17. Stock price movement.
18. Predicting stock market crash.
19. Risk assessment of insurance firm from data.
20. Identify the purchasing power using the concept of cost of living index number.
21. Identify the purchasing power using the concept of weighted aggregate price index number.
22. Calculate moving averages with the given even Periodicity. Plot them and as well as the original data on the same graph.
23. Real life application of Binomial distribution, Poisson and Normal distribution in the field of medical, games, banking, election result etc.
24. Applications of Sequence and series in Banking and Finance.

**NOTE:** No question paper for Project Work will be set by the CISCE.

## SAMPLE TABLE FOR PROJECT WORK

S. No.	Unique Identification Number (Unique ID) of the candidate	<u>PROJECT 1</u>					<u>PROJECT 2</u>					TOTAL MARKS (E + J)
		A	B	C	D	E	F	G	H	I	J	
		Teacher	Visiting Examiner	Average Marks (A + B ÷ 2)	Viva-Voce by Visiting Examiner	Total Marks (C + D)	Teacher	Visiting Examiner	Average Marks (F + G ÷ 2)	Viva-Voce by Visiting Examiner	Total Marks (H + I)	
		7 Marks*	7 Marks*	7 Marks	3 Marks	10 Marks	7 Marks*	7 Marks*	7 Marks	3 Marks	10 Marks	20 Marks
1												
2												
3												
4												
5												
6												
7												
8												
9												
10												

<b>*Breakup of 7 Marks to be awarded separately by the Teacher and the Visiting Examiner is as follows:</b>		<b>Name of Teacher:</b>	
<b>Overall Format</b>	<b>1 Mark</b>	<b>Signature:</b>	<b>Date</b>
<b>Content</b>	<b>4 Marks</b>	<b>Name of Visiting Examiner</b>	
<b>Findings</b>	<b>2 Marks</b>	<b>Signature:</b>	<b>Date</b>

**NOTE: VIVA-VOCE (3 Marks) for each Project is to be conducted only by the Visiting Examiner, and should be based on the Project only.**